



#### From Outage Probability to ALOHA MAC Layer Performance Analysis in Distributed Wireless Sensor Networks

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#### Outline

Introduction: Wireless Sensor Networks (WSNs)

Problem Statement & Outage Probability

Slotted-ALOHA *with* Channel Reservation and *Without* Interferences

Slotted-ALOHA with Channel Reservation and Interferences

Experimental Analysis and Main Result

# Introduction: Wireless Sensor Networks (WSNs)

#### Nowadays, WSNs are everywhere!



- Environmental applications.
- Home applications.
- Medical applications, etc.

#### LIRIMA PREDNET Project



Even Rhinos need smartphones!

#### Challenges behind WSNs



- ► Keep the network up for several years (5-10 years).
- ► Generally the deployed architectures are distributed ⇒ Interferences! (partially responsible for the loss of energy).

#### To face these challenges

Two directions are natural:

- Use different sources of energy (solar for example).
- Optimizing the hardware and the software.

The software concerns essentially:

- The physical layers.
- The Medium Access Control (MAC) Layer.

In this work, we study:

- The influence of the MAC layer on the network performance.
  - In particular, we address the following question:

How many channels do we need to achieve high performance distributed wireless sensor network?

# Problem Statement & Outage Probability

#### MAC Protocol: Slotted-ALOHA

- Multiple nodes and a unique BTS.
- ► Distributed access policy ⇒ the nodes make the decision (randomly) to transmit on their own (e.g. Slotted-ALOHA MAC protocol).



Multiple nodes could choose the same channel  $\Rightarrow$  Interferences!

#### Interferences quantification: Outage Probability



The probability that the signal-to-interference-plus-noise-ratio (SINR) is less than a given threshold  $\tau > 0$ ,

 $Op = \mathbb{P}\{SINR < \tau\},\$ 

where,  $SINR(o, r) = S(o, r)/(I(o) + N_0)$ .

#### Assumptions

- Π<sub>λ</sub> ⊂ ℝ<sup>2</sup> Homogeneous Poisson Point Process (HPPP) spacial distribution of the nodes with density λ.
- The wireless channel consists of path loss attenuation with no fading:

$$\forall X_i \in \Pi_{\lambda}, P_i = P_e \|X_i\|^{-\alpha},$$

where  $\alpha$ ,  $P_e > 0$ .

The Medium Access Control strategy is a Slotted-ALOHA, the communicating nodes have a density λ\* s.t.

$$\lambda^* = \frac{2T_s}{T} \frac{1}{N_c} \lambda.$$

#### Expression of Op

#### Proposition

The Outage probability for Slotted-ALOHA MAC protocol is given by the following expression:

$$Op^{SA} \equiv \lim_{N \to +\infty} \frac{1}{N} \sum_{j=1}^{N} \mathbb{I} \langle \Sigma_{\alpha}^{j} > \frac{\xi}{(\lambda^{*}\pi)^{\alpha/2}} \rangle$$

where  $\mathbb{I}\langle .\rangle$  is the indicator function,  $\xi=\frac{r^{-\alpha}}{\tau}-\frac{N_0}{P_e}$  and

$$\begin{split} \Sigma_{\alpha}^{j} &= \log\left(\frac{1}{1 - U_{0}^{j}}\right)^{-\alpha/2} \\ &+ \sum_{k=1}^{+\infty} \left(-kW_{0}\left[-\frac{1}{k}\exp\left(\frac{\log\left[(1 - U_{k}^{j})k!\right]}{k}\right)\right]\right)^{-\alpha/2} \end{split}$$

# Slotted-ALOHA *with* Channel Reservation and *Without* Interferences

# MAC Protocol Description: Slotted-ALOHA with Channel Reservation (SACR)



Assuming  $N \sim Poiss(\mu = \frac{N_n}{N_{ts}N_{fc}})$ , the reservation probability is

 $Rp = \mathbb{P}\{N = 0\} = e^{-\mu}$ 

#### SACR Strategy Illustration

BTS
Communicating node
Inactive nodes

#### Communicating Node States Modeling: Markov Chain



#### Communicating Node States Modeling: Markov Chain

Given its transition matrix  $\Gamma$ , the distribution over states is given by a stochastic row vector  $\pi$  s.t.  $\pi^{(k+1)} = \pi^{(k)}\Gamma$  and so  $\pi^{(k)} = \pi^{(0)}\Gamma^k$ , thus  $\pi^{\infty} = \pi^{(0)} \lim_{k \to \infty} \Gamma^k$ . In particular the success transmission likelihood is given by

$$Tx_i = \left[\lim_{k \to \infty} \Gamma^k\right]_{(1,4i)}$$

#### Communicating Node States Modeling: Markov Chain



Number of nodes

Figure 1: Curves of  $Tx_i$ 's.

# Slotted-ALOHA *with* Channel Reservation and Interferences

#### When interfering nodes in the out range of the BTS



where R denotes the range of the BTS.

#### When interfering nodes in the out range of the BTS



Figure 2: Comparison of the transmission success likelihood after one trial with no interfering nodes (in blue) and with interference (in black).

# Experimental Analysis and Main Result

#### Experiment using Fit-IoT-Lab platform



#### IoT-LAB: a very large scale open testbed

IoT-LAB provides a very large scale infrastructure facility suitable for testing small wireless sensor devices and heterogeneous communicating objects.

#### Experiment details

Density of nodes	$\lambda = 1.7 \cdot 10^{-6}$
Attenuation coeff.	$\alpha = 2.2$
Noise power	$N_0 = -100 dBm$
Trans. power	$P_e = 25 dBm$
SINR thresh.	au = -10 dB
Dist. node	r = 50m
Numb. nodes	$N_n = 40$
Numb. channels	$N_c = 5$
Numb. time-slots	$N_{ts} = 4$





#### Theory vs Experiments



Figure 3: Comparison between the theoretical transmission likelihood and its practical estimation for 20 channels. Best view in color.

Main result: How many channels do we need to a achieve high performance distributed wireless sensor network?



Figure 4: Transmission success likelihood in terms of number of nodes in the network and number of channels assuming the presence of interfering nodes in the out range of the BTS.

### Thank you for your attention!